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# Improving nurse scheduling using a random forest algorithm to predict employee well-being

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ii

**Abstract :** This paper introduces a new approach to nurse scheduling that integrates employee wellbeing into the decision-making process. A random forest regressor is trained to estimate a well-being score for each nurse, leveraging data from previous work weeks and considering multiple factors related to past schedules. This score is incorporated into a mixed-integer linear programming model to guide the assignment of shifts, aiming to better align schedules with individual needs. Nurses with lower well-being scores are prioritized for reduced overtime and increased shift preferences, promoting a fairer distribution of workload. The proposed method generates schedules that balance operational requirements with employee health, potentially mitigating fatigue and absenteeism.

**Keywords:** Nurse scheduling, linear integer programming, optimization, random forest regressor, employee absenteeism, prediction

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# 1 Introduction

Nurse scheduling is a difficult task for many reasons. In the province of Québec, one of the main drawbacks is that the nurses are unionized, thus the scheduling is rigid, and must follow many rules leaving very little opportunity to modify the current methodology. It is also well documented that there is currently a shortage of nurses to provide sufficient care to the patients. Of course, the COVID-19 pandemic has exacerbated the problem. In [7], the authors noticed that 25% of a 891 nurse sample were in a distress situation, caused by high pressure and a lack of resources. A recent paper [18] notes that 47.9% of nurses in their study suffered from anxiety troubles and burnout. The actual nurse shortage is caused by many factors, mainly by budget cuts and management restricted by rigid union rules.

These numbers show that nurse scheduling should be improved in order to satisfy the employees. In order to increase well-being, the authors of [19] explain that schedules should be more flexible. In the province of Québec, a schedule consists of 14 days on three shifts. The manager starts planning the schedule 8 weeks before it is available to the nurses. Therefore, nurses need to send their workdays preferences at least 6 weeks before the beginning of the new schedule, and the schedule is available 4 weeks before the first day. Creating the schedules is a tedious task, since most of the schedule is done manually and calling lists are used to fill in the blanks. Then, the overtime is planned, still using calling lists and the process is repeated until the schedule is conform to the collective agreement. Although the schedule is planned, nurses may not show up for their shift, leading to forced overtime. The risk of errors increase when the nurses work longer than their initial shift. In fact, authors of [16] observe that the risk increases after a 8.5 hour shift, and that the risk triples when they work more than 12.5 hours.

Nurse scheduling is widely studied in the literature, mainly by proposing mixed-integer linear programming models that build schedules around a set of constraints and different objectives. In [20], the objective function maximizes the number of days off. Nurses have different qualifications and can only work in certain areas. The proposed solution satisfies the nurse quotas for every shift and when compared to the manual schedule, the working hours are more fair. The authors of [2] used a branch-and-cut solver to generate nurse schedules for a one month horizon. Many constraints allow a violation and are used to avoid work overload. Results on real data from a hospital unit show that the schedule obtained by the solver considers constraints that are difficult to take into account manually, leading to a better planning. A two-phase approach is proposed in [8]. In the first phase, a schedule is proposed, then, the preferences for different shifts are taken into consideration in the second phase. Different levels of days off such as funerals, weddings, vacation and ordinary days off are considered and preferences are assigned given the different levels. The test case consisted of 20 nurses, and results show that most of the requests for days off were considered in the final planning.

As the scheduling problems contain many variables and constraints, many heuristics methods are proposed in the literature to obtain solutions faster. The authors of [11] build a schedule for regular nurses and nurses that do not have a fixed position. The heuristic, implemented easily in an Excel worksheet, allows to find a schedule that respects preferences and equity. Although obtaining a solution is quicker with a commercial optimization solver, in practice, Excel is a better solution for the managers since it does not require expertise in optimization. A multiobjective algorithm is proposed in [22] to assign nurses to operating rooms. The algorithms minimizes the makespan, which is the time length between the entry of the first patient and the output of the last patient, and maximizes the throughput, which is the total number of operations conducted. An ant colony algorithm [5] is used. Results are compared with two other studies [13, 21] and authors conclude that their solution proposed an optimal makespan and has a better balance in the allocated resources. Also, a comparable number of operations is conducted and yet, nurses have a reduced number of working hours. The proposed studies in the literature are interesting, but all used either optimization model or heuristics to obtain solutions. Moreover, as noted by [7], better planning is necessary to propose better schedules to the nurses.

In this paper, we propose to predict the well-being of nurses using a Random Forest Regressor (RFR) algorithm. The scheduling is conducted using a mixed-integer linear problem, but a parameter of the optimization model is predicted using the RFR algorithm.

Machine learning tools are efficient to predict an output based on input data. In the prediction of absenteeism, machine learning tools have been widely used [1, 9, 10]. According to the literature on the absenteeism prediction, most of the papers dealing with that theme have been published after 2018 [14]. In addition, more than the half of the works exploited regression methods, one thirds used classification methods and the rest applied clustering methods [14]. For example, Lima et al. [12] attempted to predict absenteeism of public Brazilian security agents by exploiting deep models. More specifically, the objective was to identify workers prone to long-term absenteeism. This work is based on a dataset of 6 years of professional data. Also, the deep models that have been exploited are a MultiLayer Perceptron (MLP), Recurrent Neural Network and Long Short-Term Memory. It should be noted that those three models have been compared to a baseline Support-Vector Machines classifier. The best results were obtained with MLP and when the 6 years of data have been considered for training and testing the model. Indeed, MLP reached an accuracy of 78.42%.

Random Forest (RF) algorithms are a collection of decision trees. Each tree is a weak learner, but when combined, they form a strong learner. Moreover, using bootstrap sampling allows to create multiple input data sets in order to train a robust predictive model. RF are non-parametric supervised learning algorithms that rely on the divide and conquer paradigm, more precisely by branching on attributes until a leaf node is reached. RF can be used for classification or regression and has been used successfully for the prediction of absenteeism [9, 17].

The originality of this work is using the history of the past work weeks of employees to predict a well-being score, which is then used in the optimization model that computes the scheduling of the employees. Employees with a bad well-being score will have better chances to be assigned to their shifts of choice, for example.

The paper is organized as follows. Sections 2 details the methodology, more precisely the RF algorithm and the MILP optimization model. Results are presented in Section 3 and concluding remarks in Section 4.

# 2 Methodology

Since it is merely impossible to change the work schedules, caused by the collective agreement in place for the nurses, this project is concerned with providing tools that can help improve the scheduling, by respecting the current restrictions.

First, available data is analyzed and used to predict the well-being of the nurses, by using a random forest algorithm. Second, this metric is used as an input parameter for the mixed-integer linear program that assigns the shifts to the nurses, based on the collective agreement constraints. This Section explains in details the random forest algorithm and the optimization model.

#### 2.1 Random forest algorithm

A random forest algorithm is used to predict the well-being score of nurses for the next two weeks, which is then used to generate the schedule by solving an optimization problem.

A random forest regressor is an algorithm that creates a machine learning model relying on and combining regression trees (base models). Hence, the resulting model is a forest of regression trees, where each tree provides an estimated value. It should be noted that a regression tree is a specific type of decision tree [4]. The difference between them relies in the way the target is determined. Indeed, the decision tree assigns the label of the majority class of instances in the leaf node, whereas a regression tree computes the average of the target values of instances in the leaf node. The number of trees in the forest is one of the hyperparameters that should be set by the user. Hence, since the random forest regressor creates multiple trees, this algorithm belongs to the family of ensemble learning methods and more precisely employs bagging, short for bootstrap aggregating [3]. The main advantage of using bagging is to reduce overfitting and to increase the stability and performances of predictions.

Figure 1 illustrates a random forest algorithm. It consists of n decision trees, each predicting the well-being score. Then, the average of the predictions from all the decision trees is taken as the predicted SC.

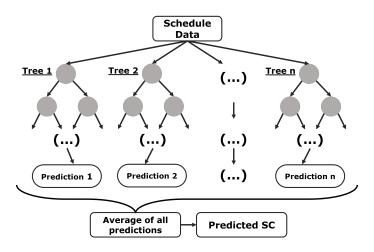


Figure 1: Random forest algorithm

The data provided to the RF algorithm, for this project, is detailed in Table 1.

Table 1: Input data to the RF algorithm

Name	Description							
Directly from historical data								
#	Employee #							
Week	Week number							
REG	# of regular shifts primary affectation							
SEC	# of regular shifts secondary affectation							
0	# of overtime shifts							
MO	# of mandatory overtime shifts							
EU	# of shifts in another nursing unit							
AI	# of shifts on sick leave							
NA	# of declared normal absence shifts							
U	# of shifts of unemployment							
DI	# of shifts on disability insurance							
Calculated from	m historical data							
CS	# of consecutive days worked, if over 5,							
	variable is equal to $-5$ , if not 0							
OVERLOAD	See Eq. $(2)$							
ER	# of extra shifts							

The goal of the RF algorithm is to predict the well-being (SC) of each nurse. To calculate this value, previous schedules are analyzed and relevant data is used to determine a score for each employee. The formula is created using knowledge in the literature, knowledge of the persons in charge of creating

G-2025-25

The formula used to predict the SC is given by:

$$SC = 10 - (10 \times F_1 \times F_2 \times F_3),$$

where  $F_1$  is related to the primary affectation of the nurse,  $F_2$  the risk of work overload and  $F_3$  the risk related to the unplanned leaves. The three values of F are all given by values  $\in [0, 1]$ , therefore  $SC \leq 10$ . The details for each value are given below.

F1. Relation with primary affectation Each nurse has a primary affectation related to her work contract, and a secondary affectation. Technically, a nurse with a day contract should always be scheduled during the day. In reality, it is sometimes difficult to obtain the work quota, therefore nurses can be affected to their secondary affectation, but with a penalty. For this project, scheduling a nurse on the secondary affectation leads to a well-being decrease. The following formula is used to calculate  $F_1$ :

$$F_1 = \frac{\text{REG} - \frac{\text{SEC}}{3}}{\text{REG}},\tag{1}$$

where REG are the number of primary affectation shifts and SEC the number of secondary affectation shifts. The value of  $F_1$  ranges between [0.67, 1], where 0.67 represents a schedule during which the nurse is always affected to her primary affection. The division by 3 is arbitrary and is chosen based on the input data. Multiple tests were conducted on the datasets and the value of 3 allows to diminish the impact of  $F_1$  on the value of SC.

F2. Risk of work overload Many factors are considered for the risk of work overload: overtime (O), mandatory overtime (MO), external unit (EU), consecutive shifts (CS) and extra shifts on regular time (ER). All these factors decrease the well-being of the nurse, since they are not part of the initial work contract.

Therefore, the variable OVERLOAD is defined:

$$OVERLOAD = O + MO + EU + CS + ER$$
<sup>(2)</sup>

All of the previous factors are considered in the formula to calculate  $F_2 \in [0, 1]$ :

$$F_2 = 1 - \frac{OVERLOAD}{20}.$$
(3)

The division by 20 is chosen since in the historical data available, the maximal score obtained for *OVERLOAD* is 16. Therefore, it could be necessary to adapt this value given the input data.

F3. Risk related to unplanned leave The factors considered in the unplanned leaves are: normal absence (NA), unemployment (U), absence due to illness (AI) and disability insurance (DI). The formula used to calculate the risk  $F_3 \in [0, 1]$  is:

$$F_3 = \left(1 - \frac{NA + U + AI + DI}{10}\right)^{1.5}.$$
 (4)

The parameter 1.5 is used to increase the impact of unplanned leaves on the final SC. As for the division by 10, the value is chosen based on the input data, since the unplanned leaves are always less or equal to 10.

#### 2.2 Optimization problem

The mixed-integer linear problem that allows to obtain a schedule to assign the nurses to the different work shifts is described in this section.

#### The **sets** are:

I:	set of nurses
$I^{int} \subset I$ :	subset of nurses in the unit
$I^{ext} \subset I$ :	subset of external nurses
$I^{inf} \subset I$ :	subset of regular nurses
$I^{aux} \subset I$ :	subset of auxiliary nurses
$J_i$ :	number of days in the schedule $i \in \{1, \ldots, 14\}$
$Q_j$ :	workshifts per day $j \in {\text{night}, \text{day}, \text{evening}}$

#### The **decision variables** are:

	$\int 1,  \text{if nurse } i \in I \text{ is affected to shift } q \in Q \text{ of day } j \in J,$
$x_{ijq} =$	0, otherwise.
4	1, if nurse $i \in I$ works overtime during shift $q \in Q$ of day $j \in J$ ,
$ts_{ijq} =$	0, otherwise.
$penalty_i =$	Penalty associated to the maximum number of shifts

#### The **parameters** are:

$Aff_{ijq} =$	$\begin{cases} 1, & \text{if nurse } i \in I \text{ can be assigned to primary} \\ & \text{affectation shift } q \in Q \text{ on day } j \in J, \\ 0, & \text{otherwise.} \end{cases}$ $\begin{cases} 1, & \text{if nurse } i \in I \text{ can be assigned to secondary} \\ & \text{affectation shift } q \in Q \text{ on day } j \in J, \\ 0, & \text{otherwise.} \end{cases}$
$Aff^{sec}_{ijq} =$	$\begin{cases} 1, & \text{if nurse } i \in I \text{ can be assigned to secondary} \\ & \text{affectation shift } q \in Q \text{ on day } j \in J, \\ 0, & \text{otherwise.} \end{cases}$
$Con_{ij} =$	$\begin{cases} 1, & \text{if nurse } i \in I \text{ requests a day off on day } j \in J, \\ 0, & \text{otherwise.} \end{cases}$
$Exp_i =$	$\begin{cases} 1, & \text{if nurse } i \in I \text{ has an expertise,} \\ 0, & \text{otherwise.} \end{cases}$
$Pref_{ijq} =$	$ \begin{cases} 0, & \text{otherwise.} \\ 1, & \text{if nurse } i \in I \text{ requests a day off on day } j \in J, \\ 0, & \text{otherwise.} \\ 1, & \text{if nurse } i \in I \text{ has an expertise,} \\ 0, & \text{otherwise.} \\ 1, & \text{if shift } q \in Q \text{ is a preference for nurse } i \in I \\ & \text{on day } j \in J, \\ 0, & \text{otherwise.} \end{cases} $
$SC_i =$	Value of the well-being metric predicted by the random forest
$B^{inf} \in I^{inf}$ and $B^{aux} \in I^{aux} = Max_i = QQ_{jq} =$	algorithm for nurse $i \in I$ Minimal number of shifts per nurse Maximal number of shifts per nurse $i \in I$ according to contract. Minimal number of nurses on shift $q \in Q$ on day $j \in J$ .

The objective function consists in maximizing the number of nurses affected to the schedule, in order to schedule the nurses to all the shifts. The first term aims at giving preferences to nurses with a high well-being score. The second term is concerned with the secondary affectations, therefore a penalty is applied for every secondary affectation. The third term penalizes overtime shifts. The fourth term penalizes largely the model when external nurses to the unit must complete the work quota. Finally, the fifth term is related to the maximal number of shifts worked by a nurse.

$$\max_{x,t,penalty} \sum_{i \in I^{int}} \sum_{j \in J} \sum_{q \in Q} ((x_{ijq} \times Pref_{ijq} \times SC_i) - (x_{ijq} \times Aff_{ijq}^{sec} \times 100) - ts_{ijq} \times SC_i \times 400)) - \sum_{i \in I^{ext}} \sum_{j \in J} \sum_{q \in Q} (x_{ijq} \times 10000) - \sum_{i \in I} (penalty_i \times SC \times 35)$$
(5)

s.t.

$$\sum_{q \in Q} x_{ijq} \le 1 \qquad \forall i \in I, j \in J, \tag{6}$$

$$\begin{aligned} x_{ijq} \le Aff_{ijq} & \forall i \in I^{int}, j \in J, q \in Q, \quad (7) \\ x_{ij} \le Aff_{sec}^{sec} & \forall i \in I^{int}, j \in J, q \in Q, \quad (8) \end{aligned}$$

$$x_{ijq} \le Aff_{ijq}^{sec} \qquad \forall i \in I^{int}, j \in J, q \in Q, \quad (8)$$

$$\sum_{j \in J} \sum_{q \in Q} x_{ijq} \le Max_i - \sum_{j \in J} Con_{ij} \quad \forall i \in I^{int},$$
(9)

$$x_{ijq} < Con_{ij} \qquad \forall i \in I^{int}, j \in J, q \in Q, (10)$$
  
$$ts_{ijq} < Con_{ij} \qquad \forall i \in I^{int}, j \in J, q \in Q, (11)$$
  
$$\sum_{q \in Q} x_{ijq} + \sum_{i \in I} con_{ij} \ge B^{inf} \qquad \forall i \in I^{inf}, (12)$$

$$\sum_{j \in J} \sum_{q \in Q} x_{ijq} + \sum_{j \in J} con_{ij} \ge B^{inf} \qquad \forall i \in I^{inf},$$

$$\sum_{j \in J} \sum_{q \in Q} x_{ijq} + \sum_{j \in J} con_{ij} \ge B^{aux} \qquad \forall i \in I^{aux},$$
(12)

$$Max_i + 3 - \lfloor SC_i \rfloor + penalty_i \ge \sum_{j \in J} \sum_{q \in Q} x_{ijq} \qquad \forall i \in I^{int},$$
(14)

$$\begin{array}{ll}
x_{ij1} + x_{i(j+1)2} \leq 1 & \forall i \in I, j \in J, \\
x_{ij1} + x_{i(j+1)0} \leq 1 & \forall i \in I, j \in J, \\
\end{array} \tag{15}$$

$$x_{ij0} + x_{i(j+1)2} \le 1 \qquad \forall i \in I, j \in J,$$

$$\sum_{i \in I} ((x_{ijq} + ts_{ijq}) \times Exp_i) \ge 1 \qquad \forall j \in J, q \in Q,$$
(17)
$$\forall j \in J, q \in Q,$$
(18)

$$x_{iig} + ts_{iig} < 1 \qquad \qquad \forall i \in I, \ i \in J, \ a \in Q. \tag{19}$$

$$\sum_{j \in J} \sum_{q \in Q} ts_{ijq} \le \left\lfloor \frac{8}{SC_i + 1} \right\rfloor \qquad \forall i \in I^{int},$$
(20)

$$\sum_{i \in I} (x_{ijq} + ts_{ijq}) = QQ_{jq} \qquad \forall j \in J, q \in Q,$$

$$\sum_{i \in I} x_{ij} + x_{ij} = 2 \times Eds_{ij} \qquad \forall i \in I$$
(21)

$$\sum_{q \in Q} x_{6jq} + x_{7jq} \equiv 2 \times F \, ds_{i0} \qquad \forall i \in I,$$

$$\sum_{q \in Q} x_{0jq} + x_{13jq} \equiv 2 \times F \, ds_{i1} \qquad \forall i \in I,$$
(22)

$$\sum_{q \in Q} x_{0jq} + x_{6jq} + x_{7jq} + x_{13jq} \le 2 \qquad \forall i \in I,$$
(24)

$$(x_{6,0,i} \times x_{7,0,i}) + (x_{6,1,i} \times x_{7,1,i}) + (x_{6,2,i} \times x_{7,2,i}) \le 2 \qquad \forall i \in I,$$

$$\sum_{q \in Q} x_{ijq} + x_{i(j+1)q} + x_{i(j+2)q} + x_{i(j+3)q} \qquad \forall i \in I,$$
(25)

$$\begin{aligned} +x_{i(j+4)q} + x_{i(j+5)q} + ts_{i(j+1)q} + ts_{i(j+2)q} \\ +ts_{i(j+3)q} + ts_{i(j+4)q} + ts_{i(j+5)q} \leq 5 \\ & x_{ijq}, ts_{ijq} \in \mathbb{B} \\ & penalty_i \in \mathbb{Z} \end{aligned} \qquad \begin{aligned} \forall i \in I, j \in J, \qquad (26) \\ \forall i \in I, j \in J, q \in Q. \quad (27) \\ \forall i \in I. \qquad (28) \end{aligned}$$

Eq.(6) ensures that nurses work only one regular shift per day. Eq.(7)–(8) are used to assign shifts to the primary or secondary affectation of the nurse. Days off are taken into account with Eq.(9)–(13). Soft constraints, represented by Eq.(14), allow to change the maximal number of shifts assigned to a nurse, given the well-being score. The collective agreement requires that after each shift worked, two shifts must remain unassigned for rest, as seen in Eq.(15)–(17). The expertise of a nurse is considered with Eq.(18) and ensures that during each shift, there is at least one nurse with an expertise. Eq.(19) are used to force the model to assign a regular or an overtime shift, not both at once. Depending on the well-being score of the nurse, Eq.(20) limits the maximal number of overtime shifts that can be assigned. Quotas of nurses during each shift are given by Eq.(21). The collective agreement in Québec imposes to work every other week-end and this is given by Eq.(22)–(25). Finally, nurses can not work more than five consecutive shifts, either in regular or overtime, as explicited by Eq.(26). Variables' domain are given by Eq.(27)–(28).

# 3 Results

This Section details the numerical results. First, the case study is presented. Then, the performance of the random forest algorithm is presented. Finally, the quality of the schedules generated by the mixed-integer linear program is analyzed.

### 3.1 Case study

The methodology and results in this paper are based on historical data provided by the Centre Intégré Universitaire de Santé et de Services Sociaux du Saguenay-Lac-St-Jean (CIUSSS SLSJ). One year of data for a specific nursing unit is available from December 2018 until December 2019. The data represents 11,314 instances, where each instance represents a work shift for one nurse. The unit is composed of nurses and auxiliary nurses and the work quotas are different for each type of nurse.

There is a total of 28 regular nurses and 12 auxiliary nurses. Schedules are constructed on a two week horizon and must respect the collective agreement, such as regular shifts, overtime, consecutive shifts, week-ends, and so forth.

Nurses are affected to a a primary shift in their work contract, but can also be scheduled to a secondary affectation. Figure 2 exposes the primary and secondary affectations of each nurse, as they are indirectly related to the quotas.

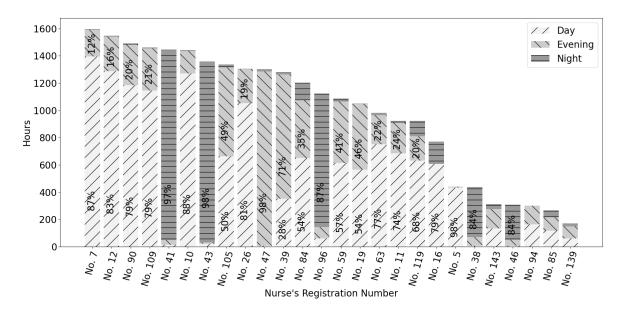


Figure 2: Primary and secondary affectations of the nurses

The analysis of the data shows that there is always less nurses available than the required quotas. Therefore, other nurses need to compensate, or the nursing unit is simply not meeting the quotas. Both situations are problematic since they increase the workload, but this is what happens in practice.

### 3.2 Random forest algorithm

The strategy leave-one-subject-out is chosen to create the training and testing sets. Therefore, all the nurses are part of the training set, except one, that is used as a testing set. This choice is motivated by the size of the datasets, which consist of 28 regular nurses and 12 auxiliary nurses. Also, as the goal of the model is to predict the well-being score of a nurse, the nurse that is analyzed is taken out of the dataset. There is a total of 535 instances available for the RF algorithm. The methodology used to train and validate the prediction of the well-being score is shown in Figure 3. As the schedule is

G-2025-25

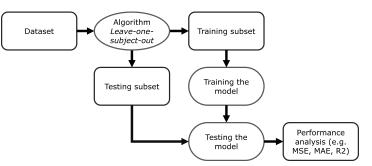


Figure 3: Training and testing sets for the RF algorithm

The Random Forest Regressor from the Sci-Kit learn library [15] is used to compute the results. The hyperparameters are also optimized using this library, and detailed in Table 2.

Table 2: Hyperparameters for the Random Forest Regressor

Parameters	Values
n_estimators	160
max_features	auto
$max_depth$	80
min_samples_split	10
min_samples_leaf	1
bootstrap	True

## 3.3 Results – Selected cases

Given the limitations on paper length, a single example for one nurse's well-being score is presented, as well as one schedule.

#### 3.3.1 Predicted score

Figure 4 shows the calculated score from historical data on the solid line and the predicted well-being score on the dashed line, for nurse 11. This nurse was on work leave from week 19 until week 33, as shown from the SC score of 0 for these weeks. One of the main takeaways of this figure is that the evolution of the score actually follow the historical data, allowing an accurate prediction of the well-being score.

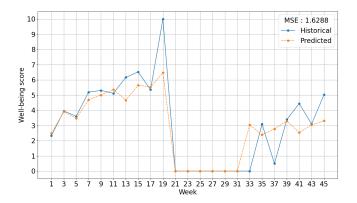


Figure 4: Nurse 11. Historical and predicted well-being (SC) score

These results show that the RF algorithm predicts correctly the tendency of the SC, even if there is a slight difference between the calculated score and the predicted score. The computation time to train the model is 11.31 seconds.

SC are calculated for all the nurses and are then used as input parameters in the optimization model.

#### 3.3.2 Schedule

The optimization model is modeled with AMPL [6] and solved with Xpress.

In order to validate results, schedules generated with the RFR and the optimization model are compared with the actual historical schedules, to determine if the proposed approach allows to enhance the current schedules. Many other tests were conducted, but for the purpose of the paper, only one case is presented.

The parameters of the optimization problem are presented in Table 3. A simple case is chosen with only two possibilities for the SC to illustrate the effect of the score on the assignments.

Parameter	Description	Value
$SC_i$	Well-Being Score	6 nurses with a score of 6
		8 nurses with a score of 1
$I^{inf}$	Number of Nurses	14
$Con_i$	Planned Leave	0
$Exp_i$	Expertise	0
$\frac{Pref_{ijq}}{B^{inf}}$	Preference	Random based of their respective work contract
$B^{inf}$	Min. Number of Assignments	8

Table 3: Parameters of the optimization model used to generate the schedule

Table 4 presents the scheduled obtained for the 14 nurses. The schedule is computed for two weeks, from Sunday to Saturday and when a letter is present, it represents a shift for the nurse. Overtime shifts are designated with \*.

Day	105	143	26	59	16	90	96	84	47	10	94	139	85	119
Sun.	$E^*$	Е	N*			D	Ν	D		D		Е		D
Mon.	D			D	Ν	D		D	Ε		Ε	Е	Ν	
Tue.	D	$\mathbf{E}$	D		Ν			D	$\mathbf{E}$		Ε		Ν	D
Wed.	D	E		D			Ν		Ε	D	Ε		Ν	D
Thu.			D	D	Ν	D	Ν	D	Ε		Ε	$\mathbf{E}$		
Fri.		E	D		Ν	D	Ν	E		D		Е		D
Sat.	D		D	D	Ν			$E^*$	Ε	$N^*$	Ε		D	
Sun.	D		D	D	Ν				E	$N^*$	Ε		D	$E^*$
Mon.	D		$\mathbf{E}$		Ν	D	Ν			D	Ε	$\mathbf{E}$		D
Tue.	D			D		D	Ν	D	Ε		Ε	E	Ν	
Wed.		$\mathbf{E}$	D		Ν	D			$\mathbf{E}$	D	Ε		Ν	D
Thu.		E	D	D	Ν				Ε	D		Ε	Ν	D
Fri.	D	$\mathbf{E}$		D	Ν		Ν	D	$\mathbf{E}$	D	Ε			
Sat.		Е	$E^*$			D	Ν	D		D		Е		DN*

Table 4: Schedule. D is for Day shift, N for Night and E for Evening. The \* represents an overtime shift

Results are presented in Table 5. The well-being score, and shift contract are presented, as well as the total number of shifts in the schedule (occurrence), the number of overtime shifts and the number of shifts of preference that are assigned, on a maximum of 10.

Results show that all the nurses with a well-being score of 6, have a lower number of assigned shifts, which is the desirable outcome. Most of the nurses also were assigned their preferred shifts. Also, the overtime shifts are not assigned to the nurses with the SC score of 6, which is also desirable. This shows that the optimization model is actually building the schedules by taking into account the well-being score of the nurses.

		Tal	ble 5:	Resul	ts	
26 50 16 00 06 84 47		10			- <b>1</b>	 

Nurse $\#$	105	143	26	59	16	90	96	84	47	10	94	139	85	119
SC	1	6	1	6	1	6	6	1	1	1	6	6	6	1
Contract	D	$\mathbf{E}$	D	D	D	Ν	D	Ε	D	D-E	$\mathbf{E}$	D	D	D
Occurrence	8	8	8	10	8	8	8	8	10	8	10	8	8	8
Overtime	1	0	2	0	0	0	0	1	0	0	2	0	0	2
Preference	7	8	6	8	0	8	7	7	9	8	9	7	1	7

# 4 Concluding remarks

This paper presents a novel methodology to create nurse schedules. A well-being score for each nurse to be assigned is computed using the past work weeks, in order to account for the fatigue of the employees. To do so, a random forest regressor is used and considers many attributes based on the last actual schedule. The goal with this parameter is to influence the optimization model, a mixed-integer linear problem that computes the schedules, in order to assign more shift preferences and less overtime, for example, to the employees that have a lower well-being score. Results show that the schedules provide fair schedules that could lead to reduced absenteeism. Future work based on this project would require actually implementing the computed schedules in a work place to assess the methodology in practice.

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